

SUPERSYMMETRIC DARK MATTER



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Fermilab Wine & Cheese
Hunt for DM Workshop

Dark Matter

- $\Omega_{\text{DM}}h^2 = 0.105 \pm 0.004$ (WMAP, SDSS)
- Best evidence for new physics
 - Unambiguous
 - Intimately connected to central problems: electroweak symmetry breaking and structure formation
- Theory: many compelling and new possibilities
 - Not baryonic (\neq weakly-interacting)
 - Not hot (\neq cold)
 - Not short-lived (\neq stable)
- Experiment, observation: bright prospects
 - Astroparticle physics: direct and indirect detection
 - Cosmology: halo profiles, CMB, BBN, ...
 - Particle physics: Tevatron, LHC

THE “WIMP MIRACLE”

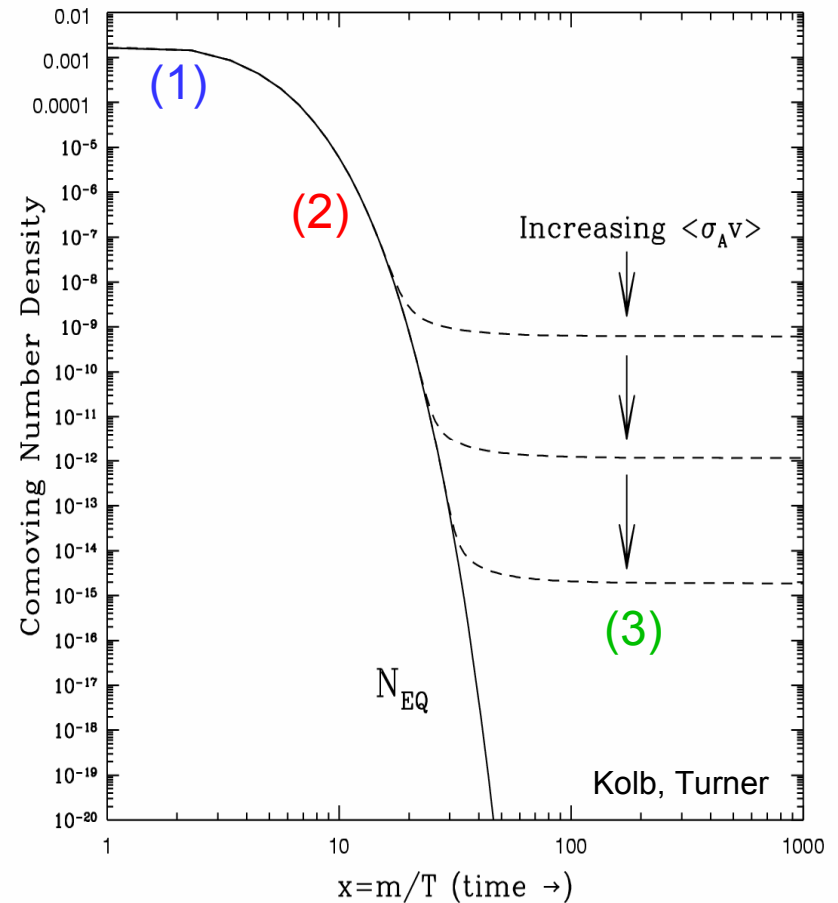
(1) Assume a new (heavy) particle χ is initially in thermal equilibrium:



(2) Universe cools:



(3) χ s “freeze out”:

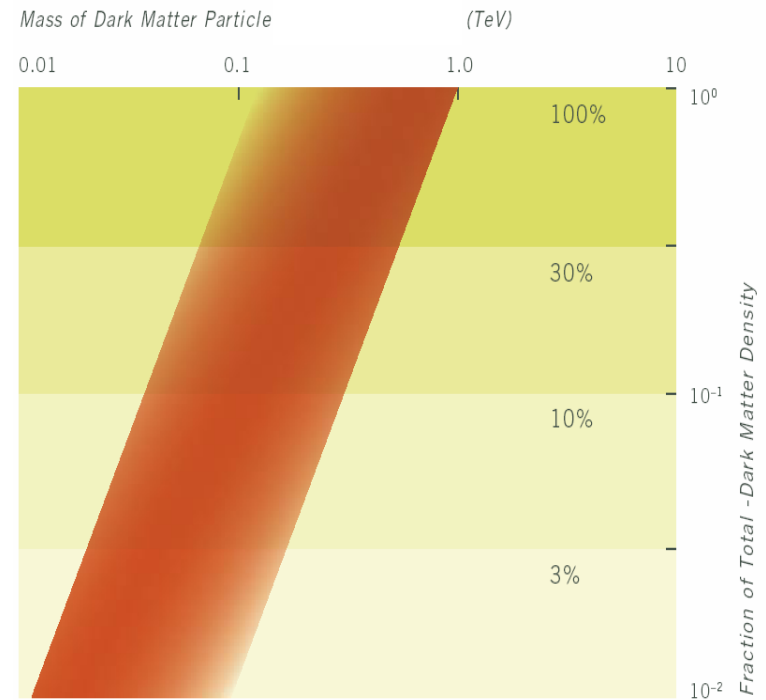


- The amount of dark matter left over is inversely proportional to the annihilation cross section:

$$\Omega_{\text{DM}} \sim \langle \sigma_A v \rangle^{-1}$$

- What is the constant of proportionality?
- Impose a natural relation:

$$\sigma_A = k\alpha^2/m^2, \text{ so } \Omega_{\text{DM}} \sim m^2$$



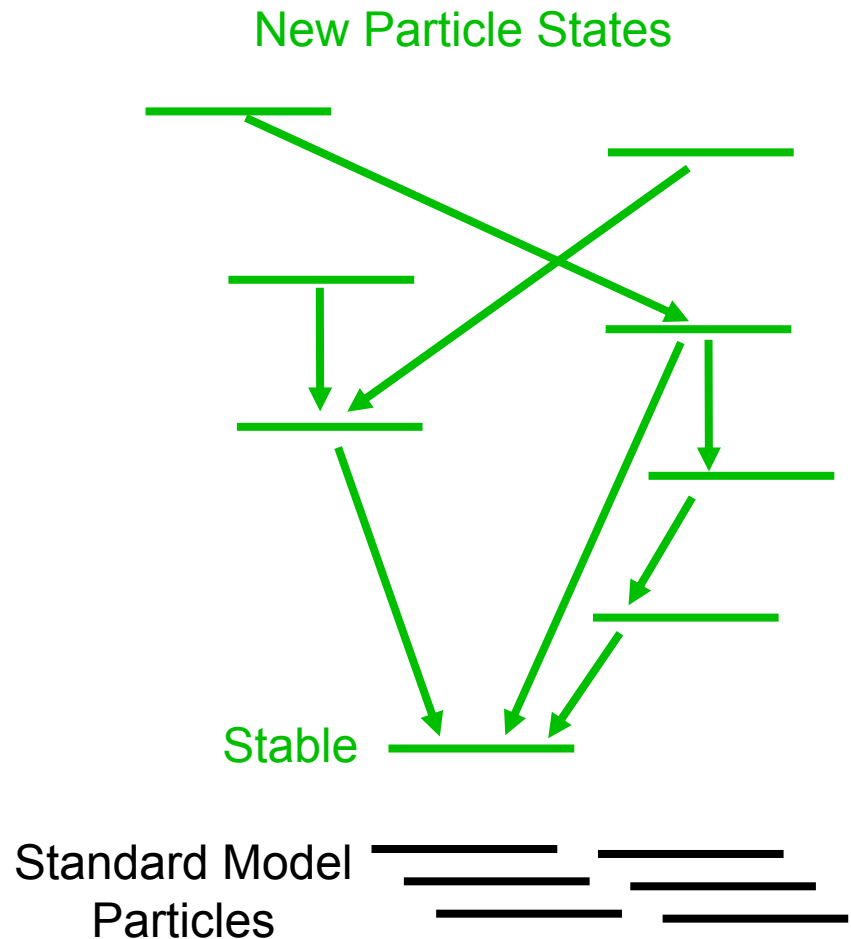
HEPAP LHC/ILC Subpanel (2006)

[band width from $k = 0.5 - 2$, S and P wave]

Remarkable “coincidence”: $\Omega_{\text{DM}} \sim 0.1$ for $m \sim 0.1 - 1$ TeV
 Cosmology alone tells us we should explore the weak scale

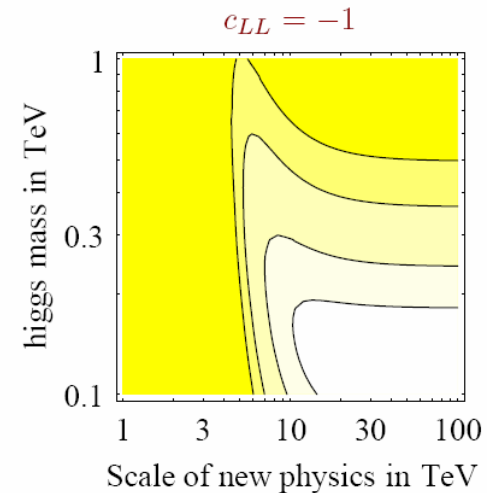
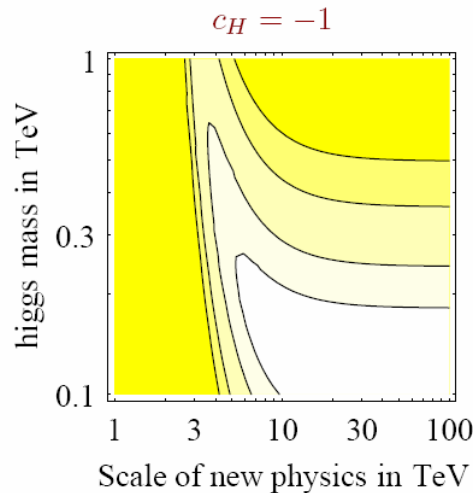
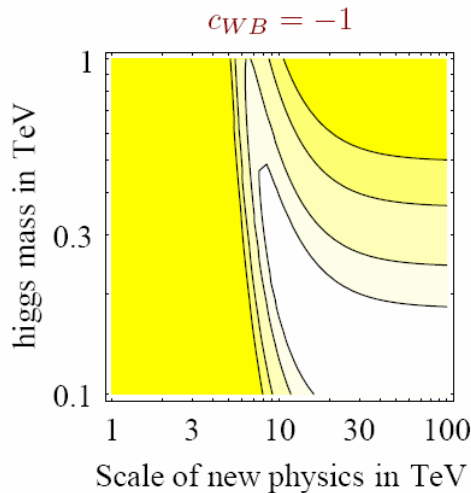
STABILITY

- This all assumes the WIMP is stable
- How natural is this?



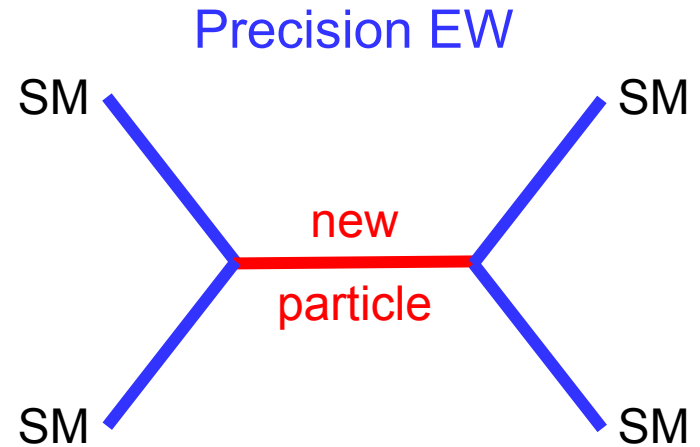
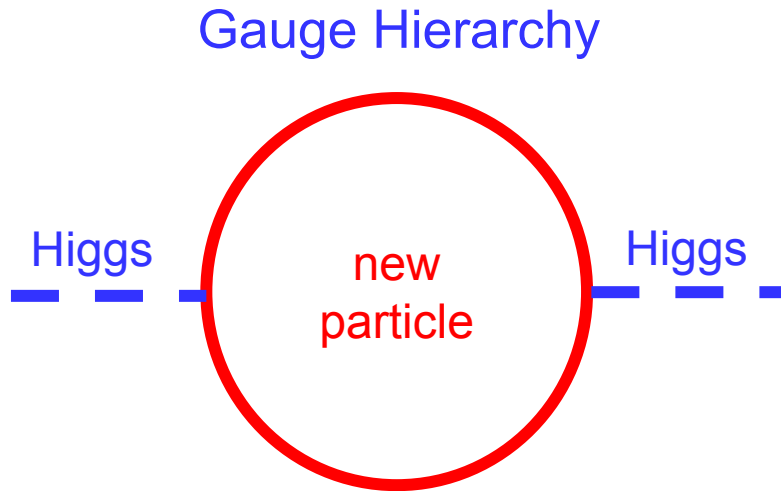
LEP

- Large Electron Positron Collider at CERN, 1989-2000
- LEP and SLC confirmed the standard model, stringently constrained effects of new particles
- Problem: Gauge hierarchy \rightarrow new particles ~ 100 GeV
LEP/SLC \rightarrow new particles > 3 TeV
(even considering only flavor-, CP-, B-, and L-conserving effects)



Barbieri, Strumia (2000)

LEP'S COSMOLOGICAL LEGACY



- Simple solution: impose a discrete parity, so all interactions require pairs of new particles. This also makes the lightest new particle stable.

Cheng, Low (2003); Wudka (2003)

- LEP's Cosmological Legacy:

LEP constraints \leftrightarrow Discrete symmetry \leftrightarrow Stability

- Dark matter is easier to explain than no dark matter
- The WIMP paradigm is more natural than ever before, leading to a proliferation of candidates

EXAMPLES

- Supersymmetry

- R-parity
- Neutralino DM

Goldberg (1983); Ellis et al. (1984)

- Universal Extra Dimensions

- KK-parity
- Kaluza-Klein DM

Appelquist, Cheng, Dobrescu (2000)

Servant, Tait (2002)

Cheng, Feng, Matchev (2002)


- Branes

- Brane-parity
- Branons DM

Cembranos, Dobado, Maroto (2003)

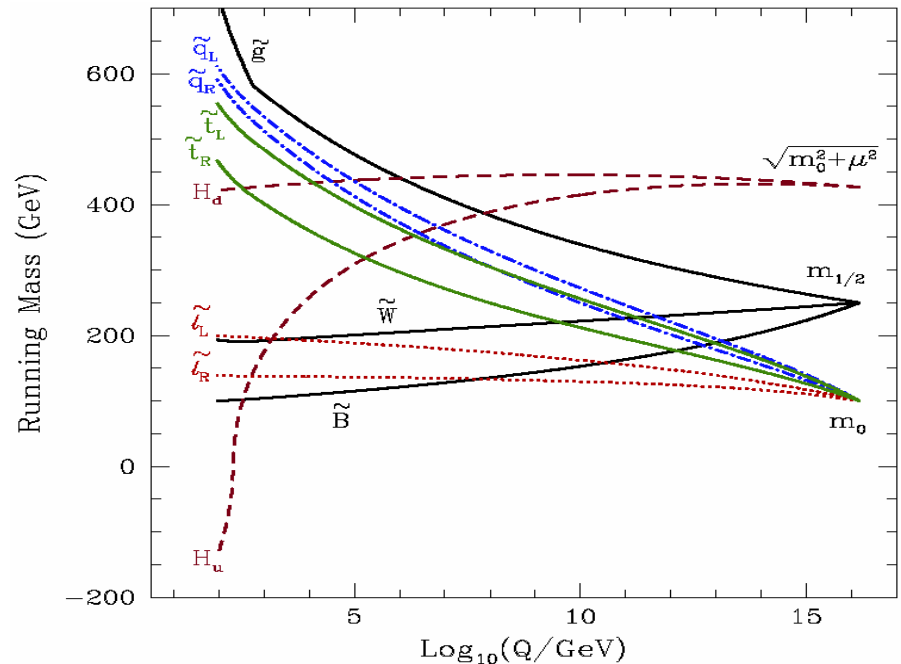
- ...

SUSY DM CANDIDATES

Spin	U(1) M_1	SU(2) M_2	Up-type μ	Down-type μ	$m_{\tilde{\nu}}$	$m_{3/2}$
2						G graviton
3/2		Neutralinos: $\{\chi \equiv \chi_1, \chi_2, \chi_3, \chi_4\}$				\tilde{G} gravitino
1	B	W^0				
1/2	\tilde{B} Bino	\tilde{W}^0 Wino	\tilde{H}_u Higgsino	\tilde{H}_d Higgsino	ν	
0			H_u	H_d	$\tilde{\nu}$ sneutrino	

NEUTRALINOS

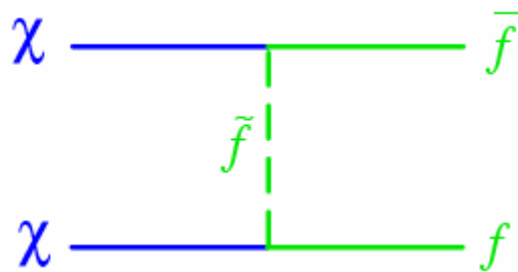
- The neutralino is the classic WIMP
 - $\sim 50 \text{ GeV} - 1 \text{ TeV}$
 - weakly-interacting
 - Naturally the lightest standard model superpartner in many models



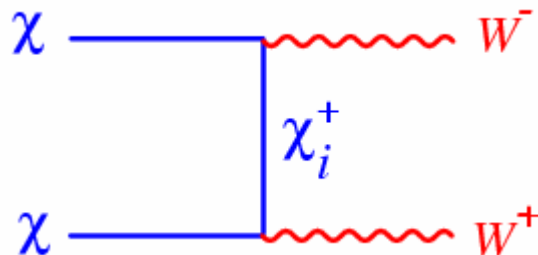
- So many SUSY models and parameters. Can we say anything interesting?

Neutralino Characteristics

- Neutralinos are sensitive to *many* processes. [→]
- But there are essentially two classes:



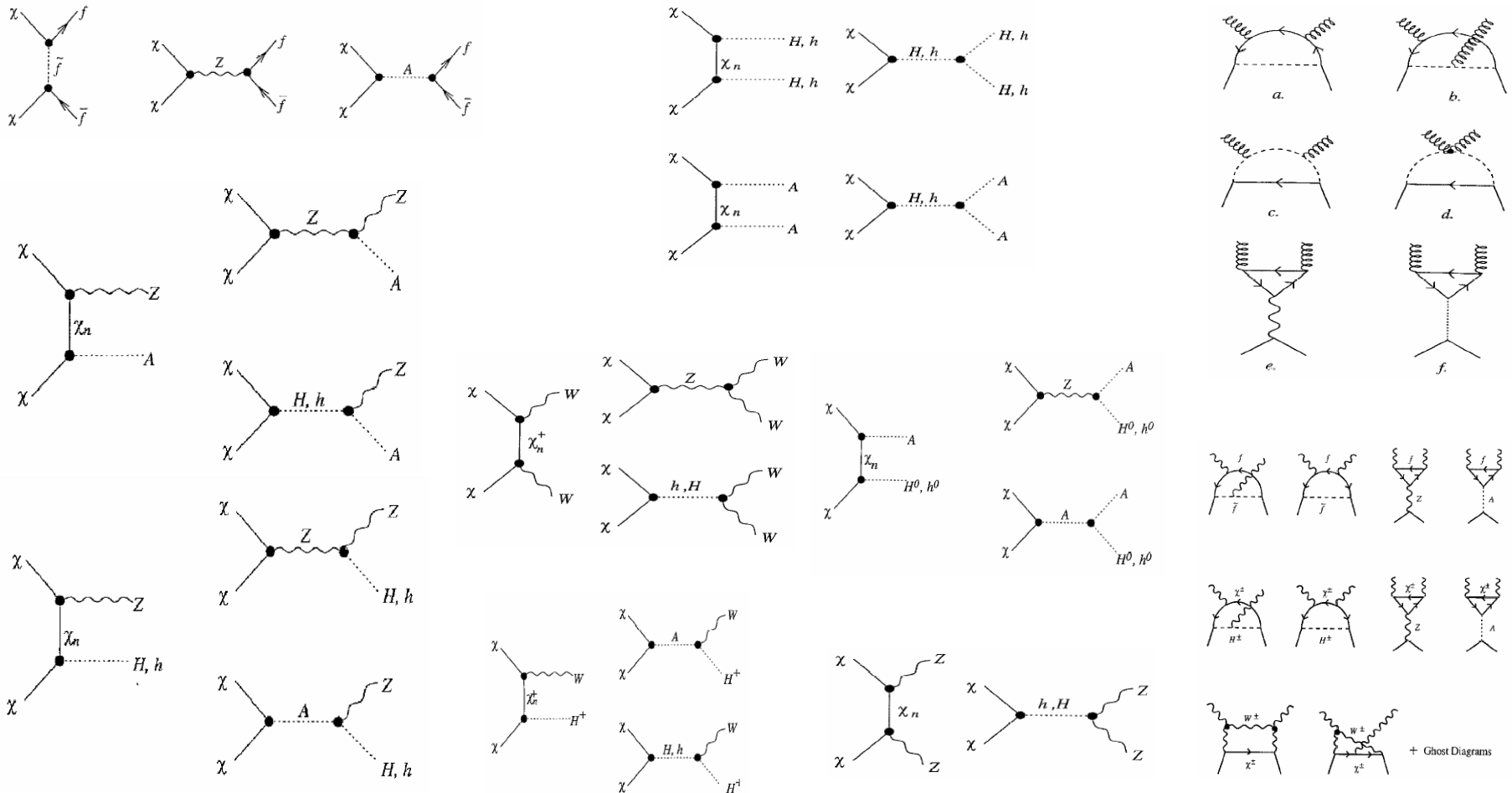
- Fermion diagrams
 - χ are Majorana fermions:
 - Pauli exclusion $\rightarrow S = 0$
 - L conservation $\rightarrow P$ wave suppression
 - m_f/m_W suppression



- Gauge boson diagrams
 - suppressed for $\chi \approx$ Bino

Bottom line: annihilation is typically suppressed, $\Omega_{\text{DM}} h^2$ is typically high

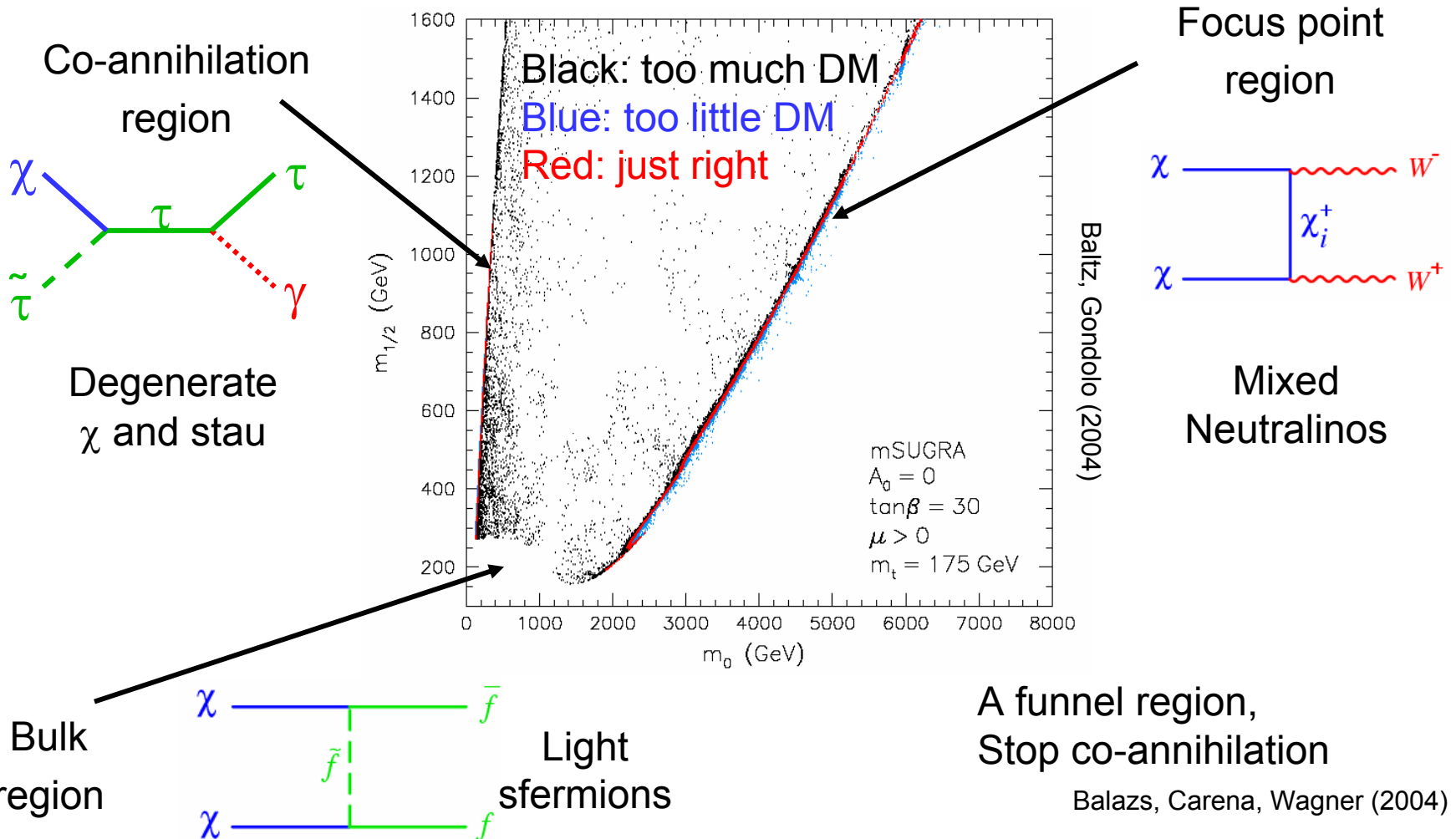
Contributions to Neutralino WIMP Annihilation



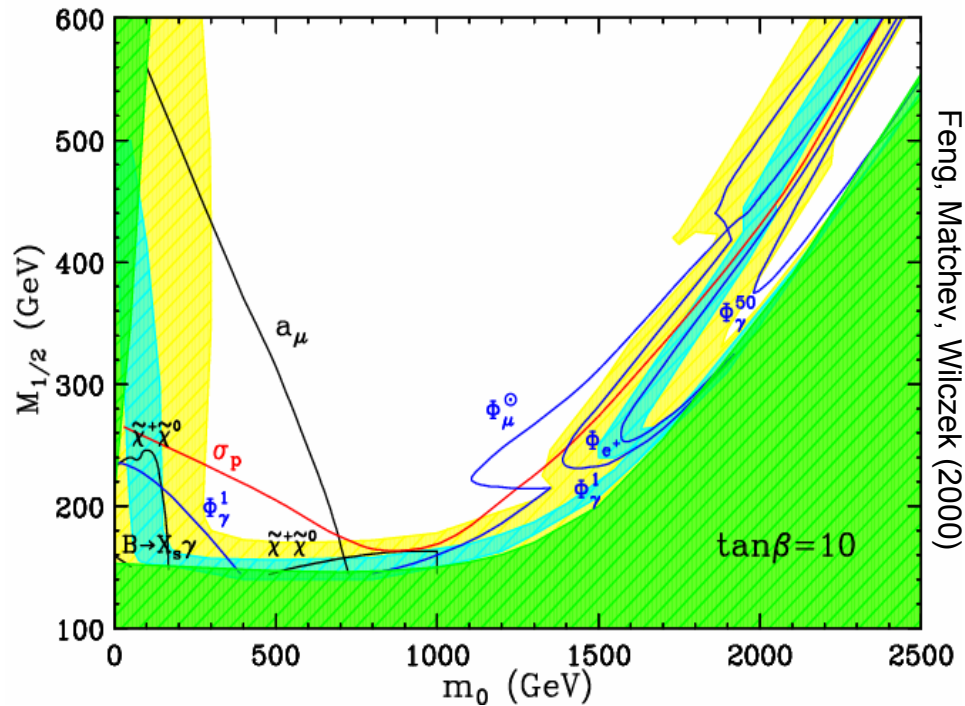
Jungman, Kamionkowski, Griest (1995)

Cosmologically Preferred Supersymmetry

$\Omega_{\text{DM}} h^2$ excludes many possibilities, favors certain models



Implications for Detection



Many diverse experiments are promising
More than one required, even in the same
category, to establish/explore signals

The View from 2000

TABLE I. Current and planned neutrino experiments. We list also each experiment's (expected) start date, physical dimensions (or approximate effective area), muon threshold energy E_μ^{thr} in GeV, and 90% CL flux limits for the Earth Φ_μ^\oplus and Sun Φ_μ^\odot in $\text{km}^{-2} \text{yr}^{-1}$ for half-cone angle $\theta \approx 15^\circ$ when available.

Experiment	Type	Date	Dimensions	E_μ^{thr}	Φ_μ^\oplus	Φ_μ^\odot
Baksan [65]						
Kamiokande [66]						
MACRO [67]						
Super-Kamiokande [68]						
Baikal NT-96 [69]						
AMANDA B-10 [70]						
Baikal NT-200 [71]						
AMANDA II [72]						
NESTOR [§] [72]						
ANTARES [73]						
IceCube [71]						

* 2 GeV for Super-Kamiokande

TABLE II. Some of the current and planned γ ray detector experiments with sensitivity to start date and details constructed for details.

Discovery prospects
“before the LHC”

E_γ Range
0.02–30
20–300
20–300
100–2,000

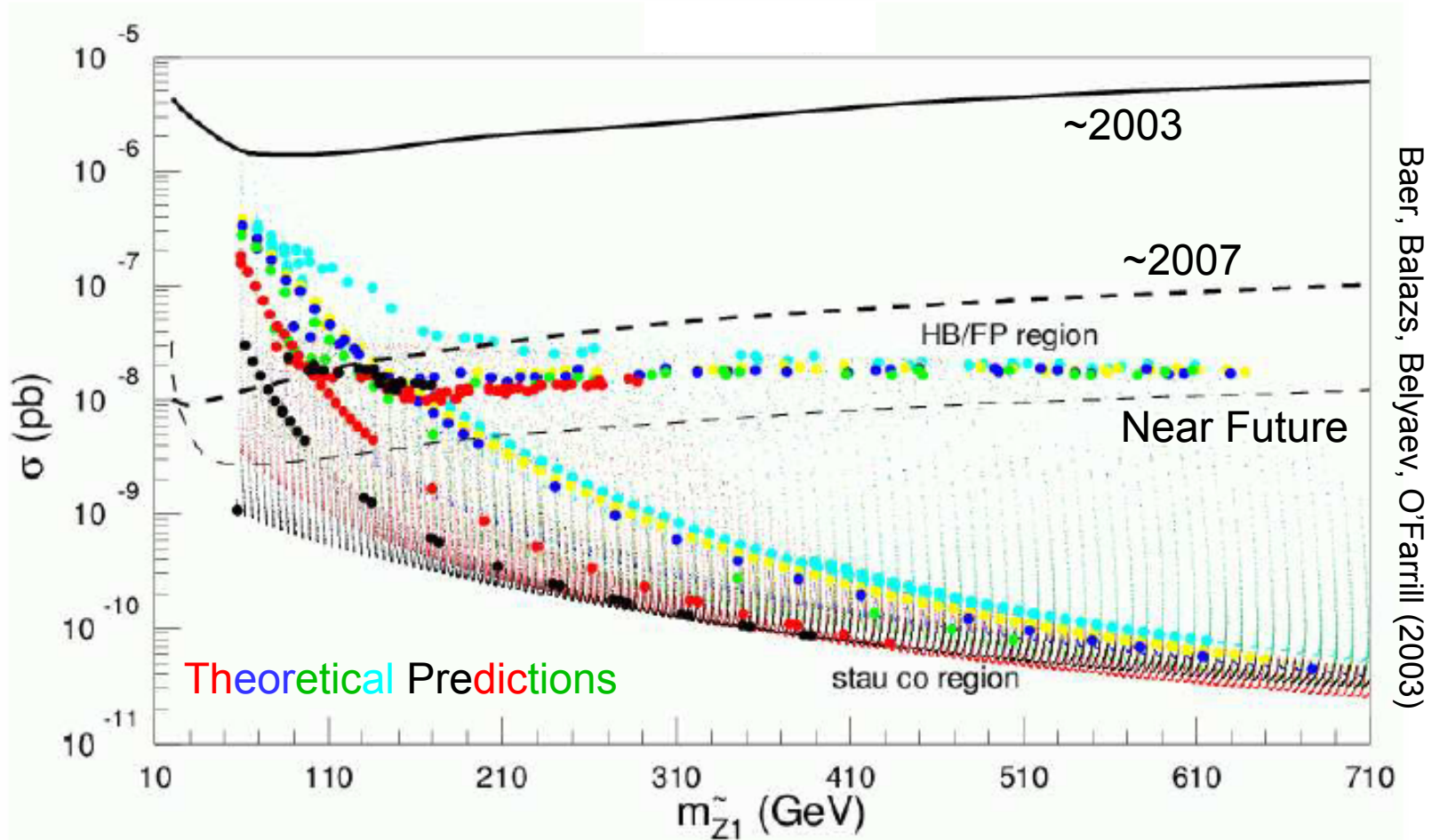
TABLE III. Recent and planned e^+ detector experiments. We list each experiment's (expected) start date, duration, geometrical acceptance in $\text{cm}^2 \text{sr}$, maximal E_{e^+} sensitivity in GeV, and (expected) total number of e^+ detected per GeV at $E_{e^+} = 50$ and 100 GeV.

Experiment	Type	Date	Duration	Acceptance	$E_{e^+}^{\text{max}}$	$\frac{dN}{dE}(50)$	$\frac{dN}{dE}(100)$
HEAT94/95 [114]	Balloon	1994/95	29/26 hr	495	50	—	—
CAPRICE94/98 [115]	Balloon	1994/98	18/21 hr	163	10/30	—	—
PAMELA [116]	Satellite	2002-5	3 yr	20	200	7	0.7
AMS-02 [117]	Space station	2003-6	3 yr	6500	1000	2300	250

A Note on Direct Detection

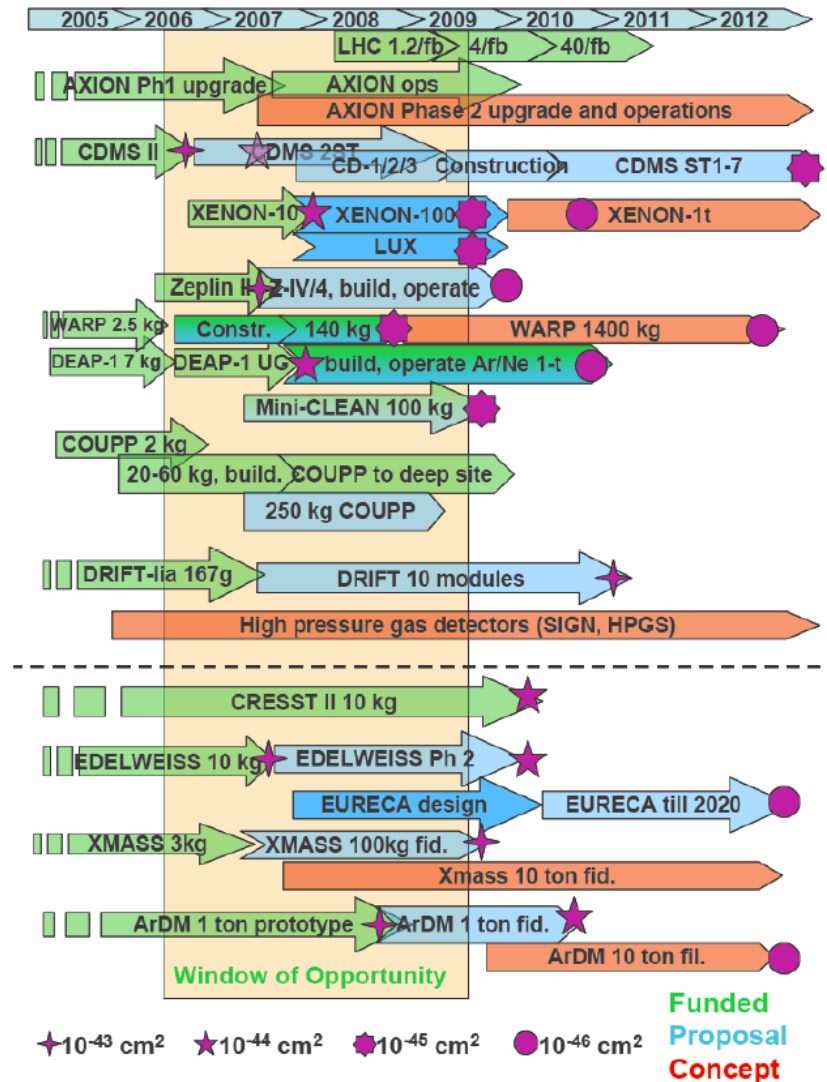
- Details are model-dependent, but there are general lessons to abstract from these considerations. For example:
- Direct detection
SUSY flavor, CP problems suggest that sleptons and squarks are heavy
 $\Omega_{\text{DM}} h^2 \rightarrow$ mixed (Bino-Higgsino, focus point) neutralinos
- This conclusion
 - holds for a wide variety of models (mSUGRA, general focus point SUSY, gaugino-mediated, more minimal SUSY, 2-1 models, split SUSY,...), constrains models that are not even cosmologically motivated
 - leads to concrete predictions

Direct Detection



10^{-8} pb (10^{-44} cm²) is an extremely significant goal for direct detection

Future Direct Detection



NEUTRALINO PROSPECTS

If neutralinos contribute significantly to dark matter, we are likely to see signals before the end of the decade:

Direct dark matter searches

Indirect dark matter searches

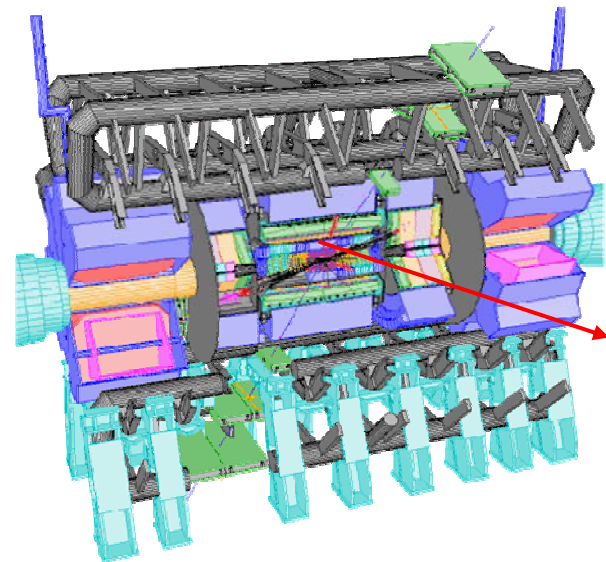
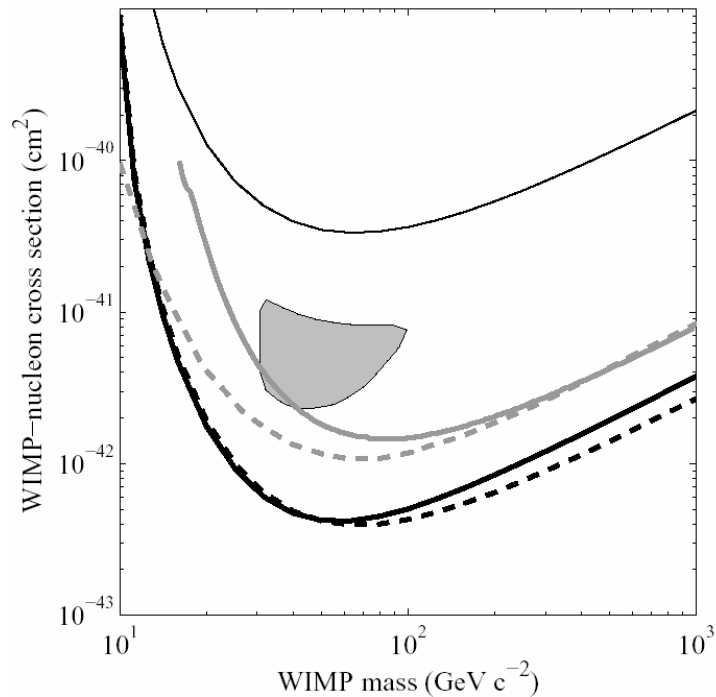
Tevatron at Fermilab

Large Hadron Collider at CERN

What then?

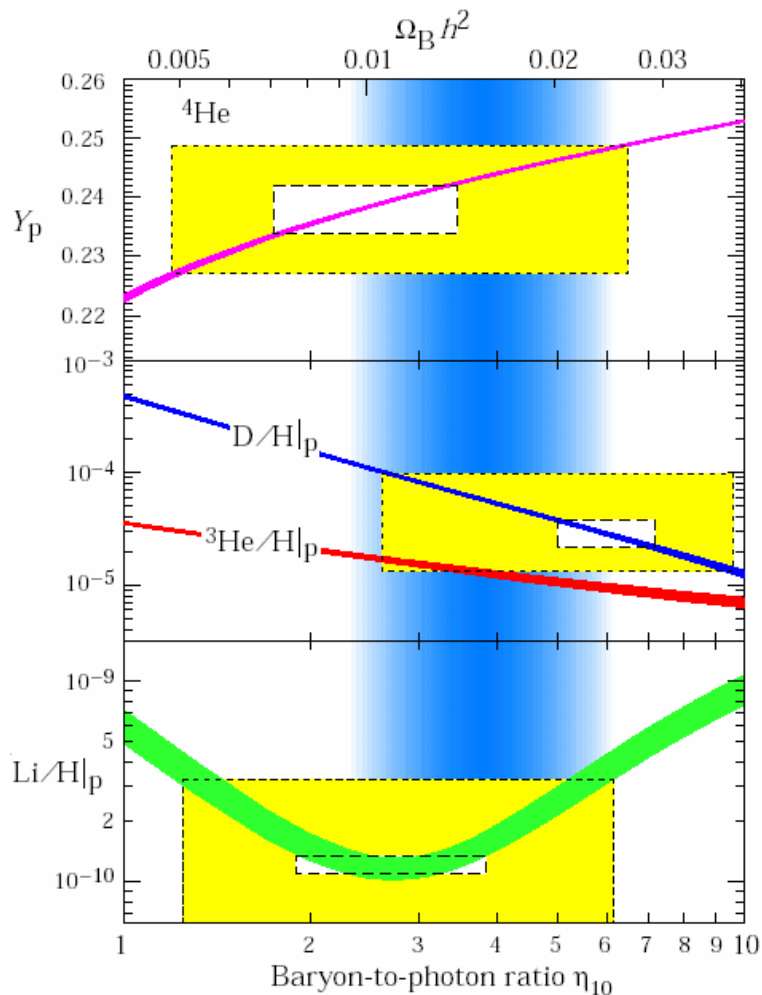
- Cosmo/astro can't discover SUSY

- Particle colliders can't discover DM



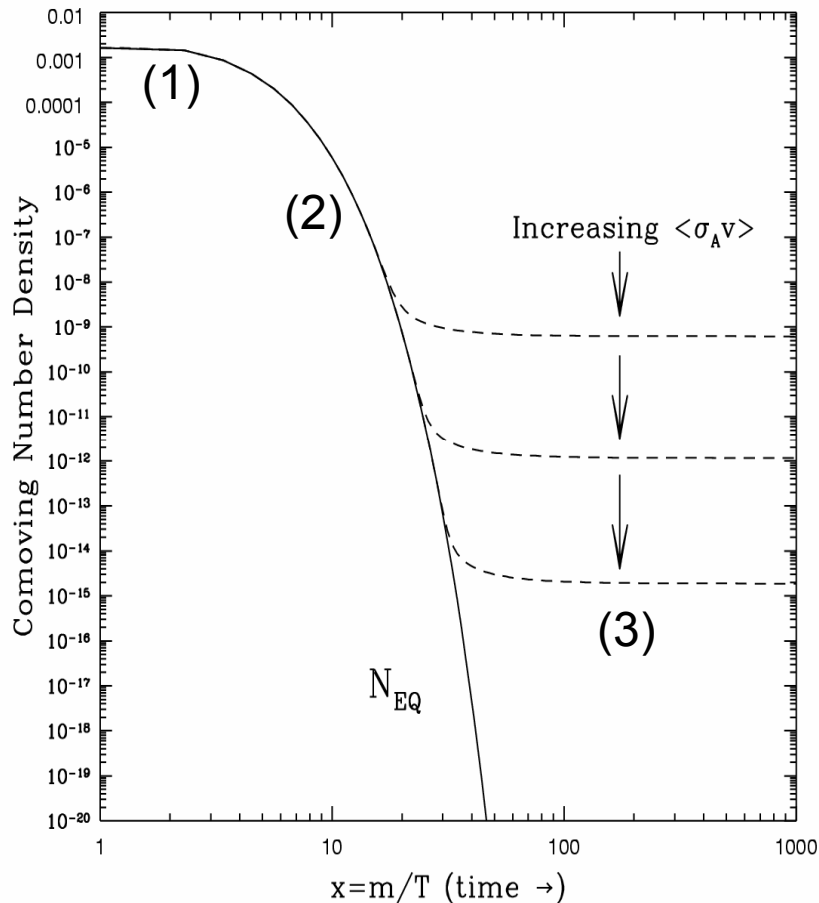
Lifetime $> 10^{-7} \text{ s} \rightarrow 10^{17} \text{ s} ?$

THE EXAMPLE OF BBN



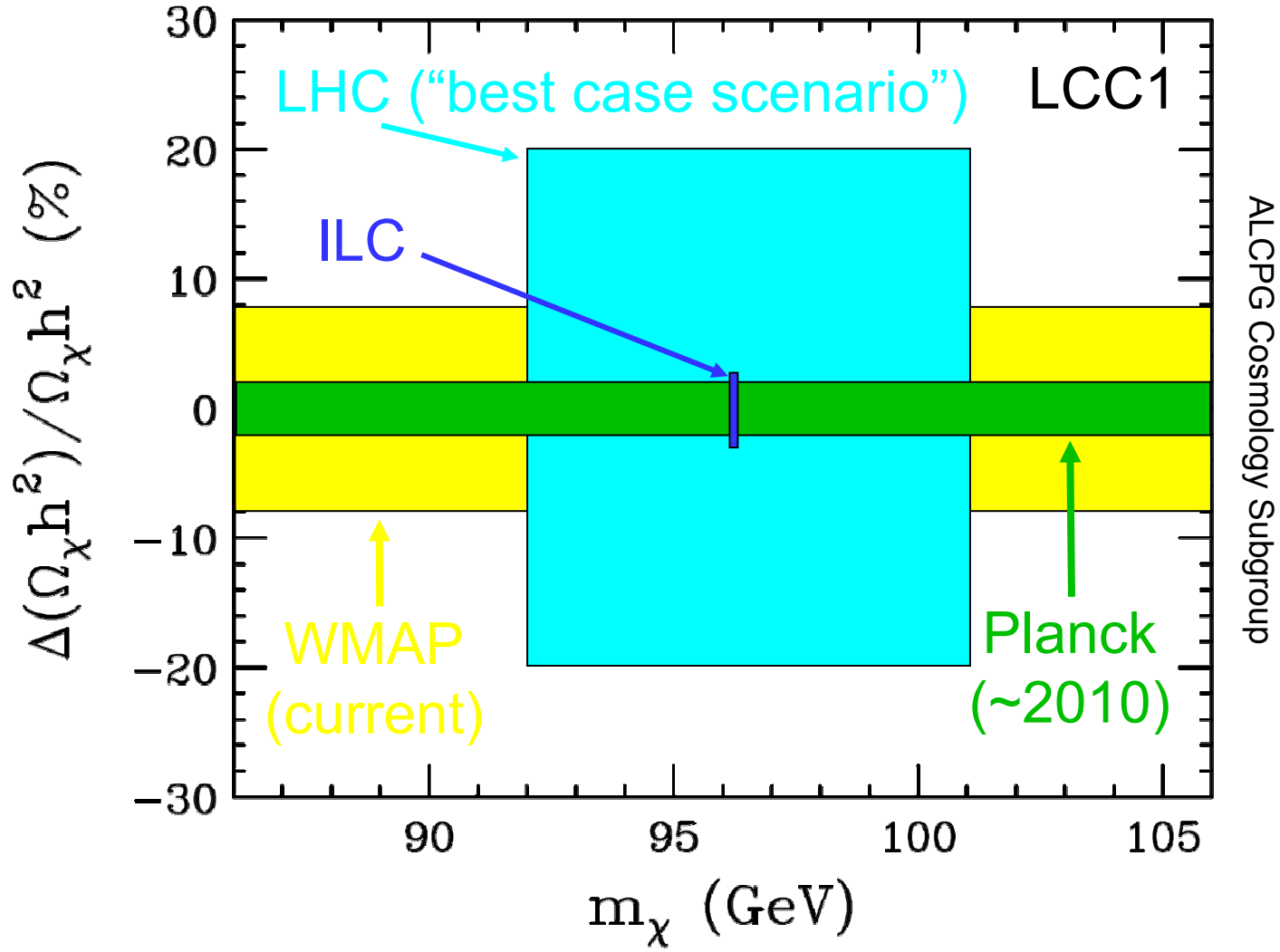
- Nuclear physics → light element abundance predictions
- Compare to light element abundance observations
- Agreement → we understand the universe back to
 - $T \sim 1 \text{ MeV}$
 - $t \sim 1 \text{ sec}$

DARK MATTER ANALOGUE



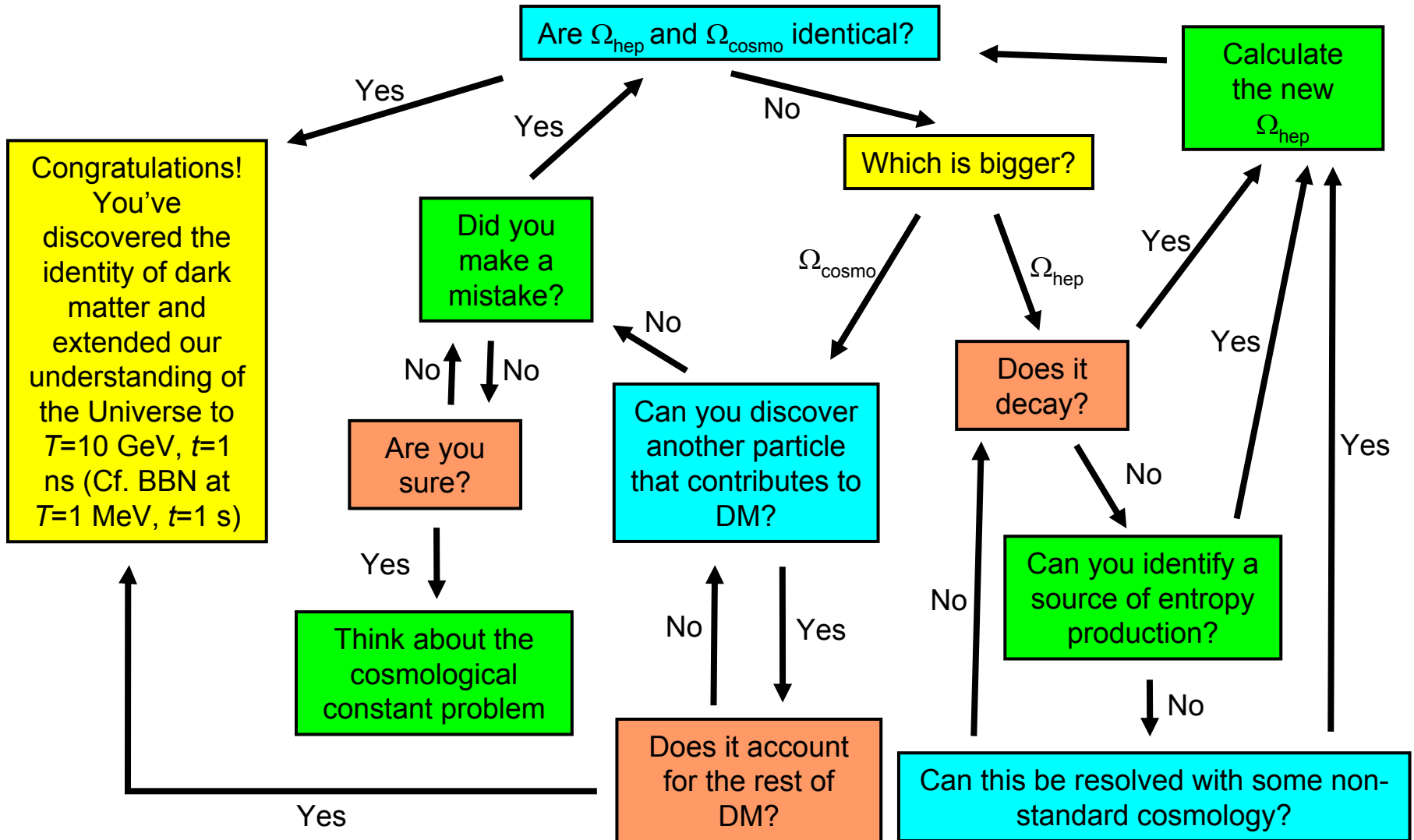
- Particle physics \rightarrow dark matter abundance prediction
- Compare to dark matter abundance observation
- How well can we do?

RELIC DENSITY DETERMINATIONS

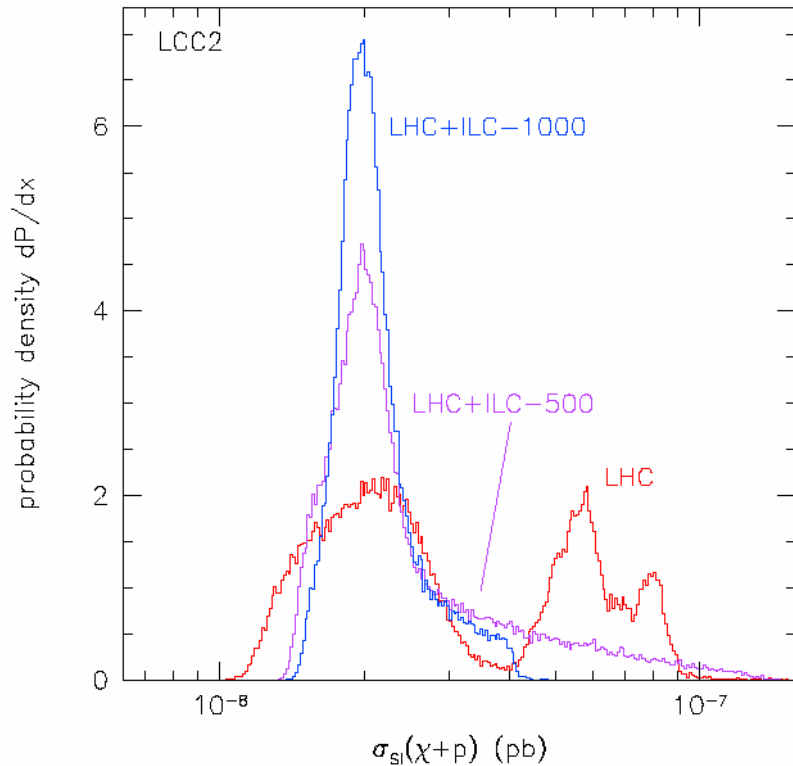


% level comparison of predicted Ω_{hep} with observed Ω_{cosmo}

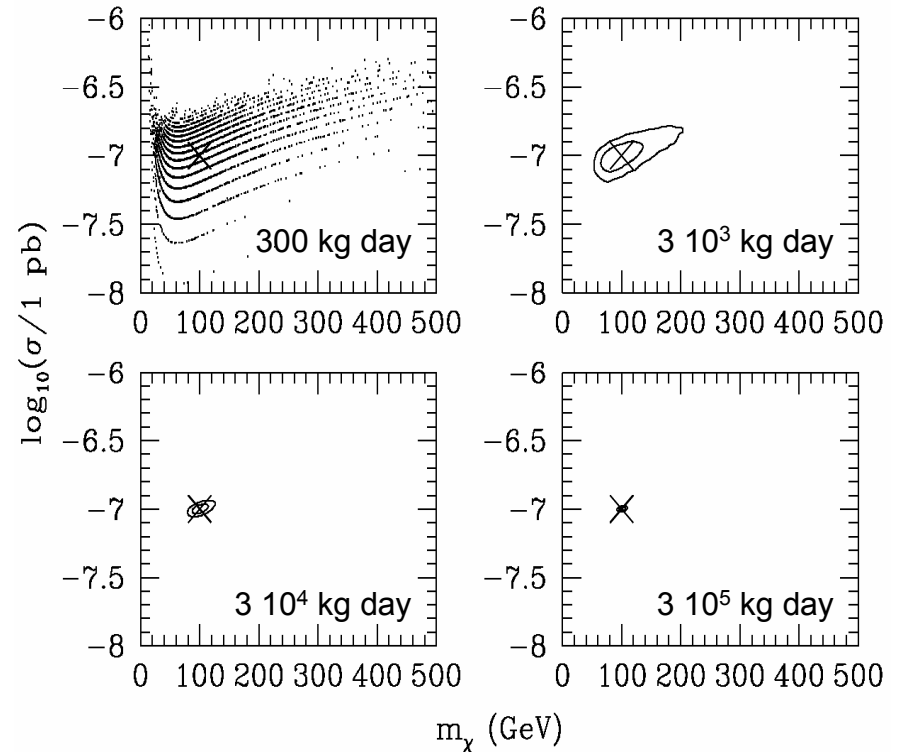
IDENTIFYING DARK MATTER



DIRECT DETECTION IMPLICATIONS



Baltz, Battaglia, Peskin, Wizansky (2006)



Green (2007)

Comparison tells us about local dark matter density and velocity profiles

INDIRECT DETECTION IMPLICATIONS



$$\frac{d\Phi_\gamma}{d\Omega dE} = \sum_i \underbrace{\frac{dN_\gamma^i}{dE} \sigma_i v \frac{1}{4\pi m_\chi^2}}_{\text{Particle Physics}} \underbrace{\int_\psi \rho^2 dl}_{\text{Astro-Physics}}$$

Gamma ray fluxes factorize

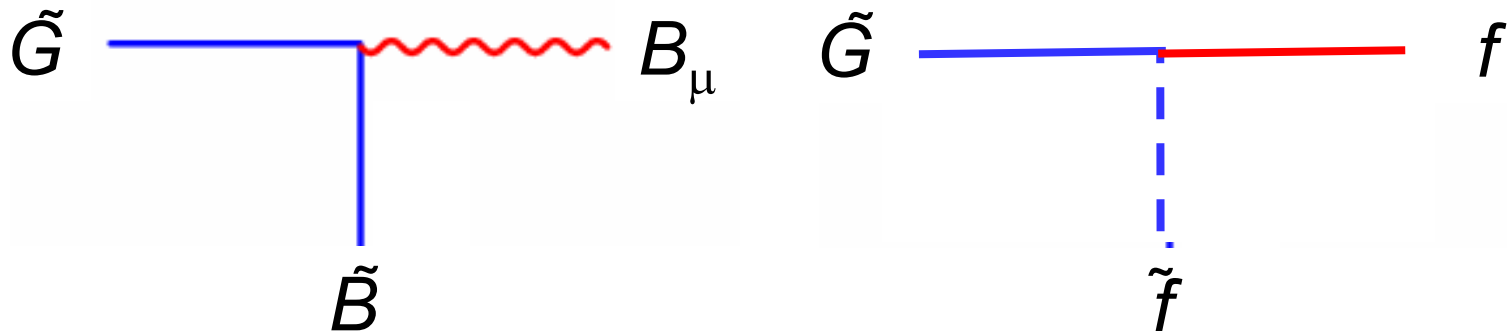
**COLLIDERS ELIMINATE PARTICLE PHYSICS UNCERTAINTIES,
ALLOW ONE TO PROBE ASTROPHYSICAL DISTRIBUTIONS**

TAKING STOCK

- Neutralinos (and all WIMPs) are
 - Weakly-interacting
 - Cold
 - Stable
- Is this true of all DM candidates?
No!
- Is this true of all SUSY candidates?
No!
- Is this true of all SUSY candidates motivated by the “WIMP miracle”?
No!

GRAVITINOS

- SUSY: graviton $G \rightarrow$ gravitino \tilde{G}
- Gravitino properties
 - Spin 3/2
 - Mass: $eV \rightarrow 100 \text{ TeV}$
 - Interactions are superweak (weaker than weak)



Production Mechanisms

- Gravitinos are the original SUSY dark matter

Pagels, Primack (1982)
Weinberg (1982)
Krauss (1983)
Nanopoulos, Olive, Srednicki (1983)

Khlopov, Linde (1984)
Moroi, Murayama, Yamaguchi (1993)
Bolz, Buchmuller, Plumacher (1998)
Baltz, Murayama (2001)

...

Classic ideas:

- Gravitinos have thermal relic density

$$\Omega_{\tilde{G}} < 1 \Rightarrow m_{\tilde{G}} < 1 \text{ keV}$$

- For DM, require a new, energy scale (and entropy production)

- Weak scale gravitinos diluted by inflation, regenerated in reheating

$$\Omega_{\tilde{G}} < 1 \rightarrow T_{\text{RH}} < 10^{10} \text{ GeV}$$

- For DM, require a new, energy scale

VIRTUES AND DRAWBACKS

- Are these acceptable scenarios?
- Strictly speaking, yes – the only required DM interactions are gravitational (much weaker than weak)
- But they are not very testable, and they aren't motivated by the “WIMP miracle,” which strongly prefers weak interactions

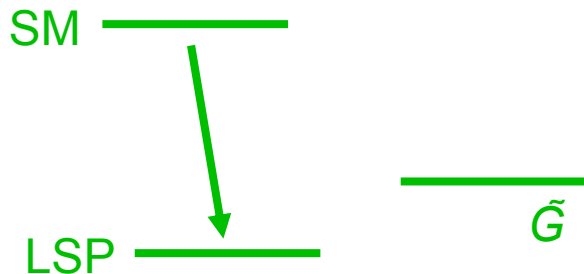
Can we fix these drawbacks?

SUPERWIMPS: BASIC IDEA

Feng, Rajaraman, Takayama (2003)

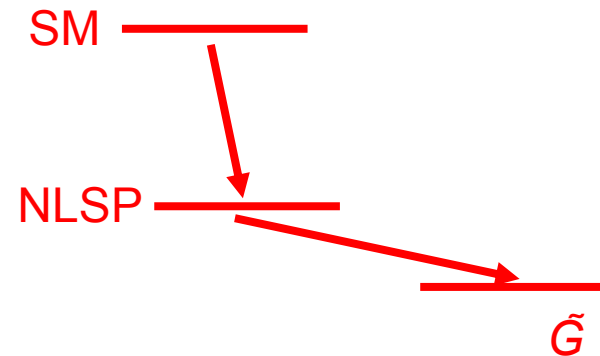
Gravitino mass ~ 100 GeV, couplings $\sim M_W/M_{Pl} \sim 10^{-16}$

- \tilde{G} not LSP



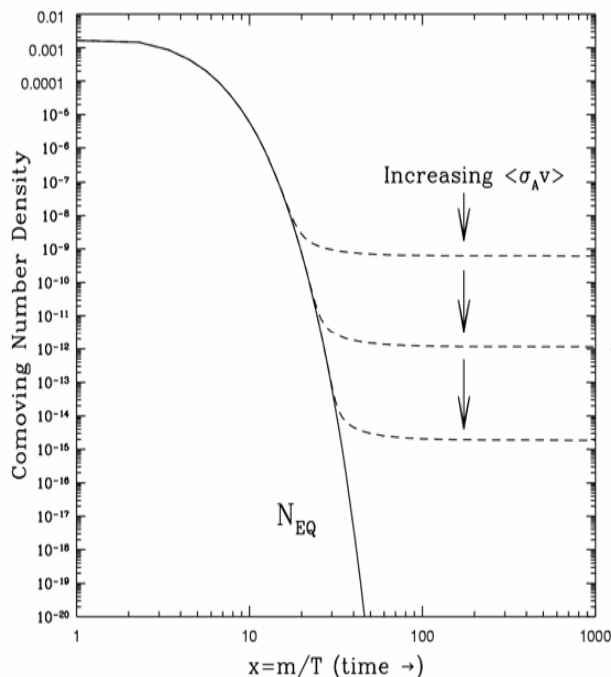
- Assumption of most of literature

- \tilde{G} LSP



- Completely different cosmology and particle physics

SUPERWIMP RELICS



- Suppose gravitinos \tilde{G} are the LSP

- WIMPs freeze out as usual

- But then all WIMPs decay to gravitinos after

$$M_{\text{Pl}}^2/M_W^3 \sim \text{hours to month}$$

Gravitinos naturally inherit the right density, but interact only gravitationally – they are superWIMPs (also axinos, KK gravitons, quintessinos, etc.)

Feng, Rajaraman, Takayama (2003); Bi, Li, Zhang (2003); Ellis, Olive, Santoso, Spanos (2003); Wang, Yang (2004); Feng, Su, Takayama (2004); Buchmuller, Hamaguchi, Ratz, Yanagida (2004); Roszkowski, Ruiz de Austri, Choi (2004); Brandenburg, Covi, Hamaguchi, Roszkowski, Steffen (2005); ...

SuperWIMP Detection

- SuperWIMPs evade all direct, indirect dark matter searches.



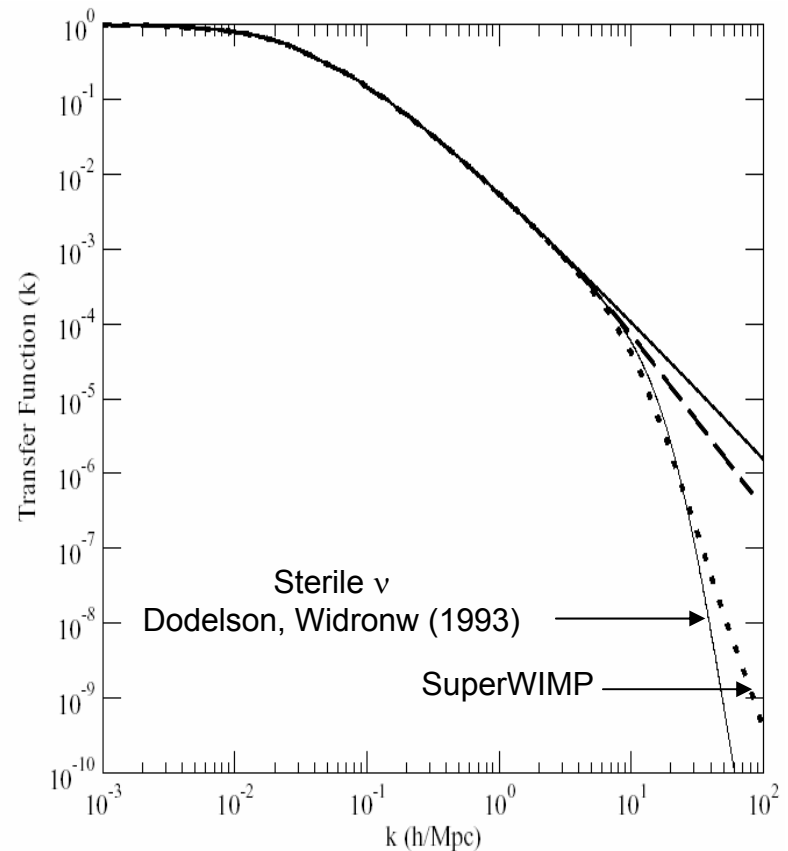
“Dark Matter may be Undetectable”

- But cosmology is complementary: Superweak interactions \rightarrow very late decays to gravitinos \rightarrow observable consequences.
- Signals
 - Small scale structure
 - Big Bang nucleosynthesis
 - CMB μ distortions

SMALL SCALE STRUCTURE

- SuperWIMPs are produced in late decays with large velocity ($0.1c - c$)
- Suppresses small scale structure, as determined by λ_{FS} , Q
- Warm DM with cold DM pedigree
- SUSY does not predict only CDM; small scale structure constrains SUSY

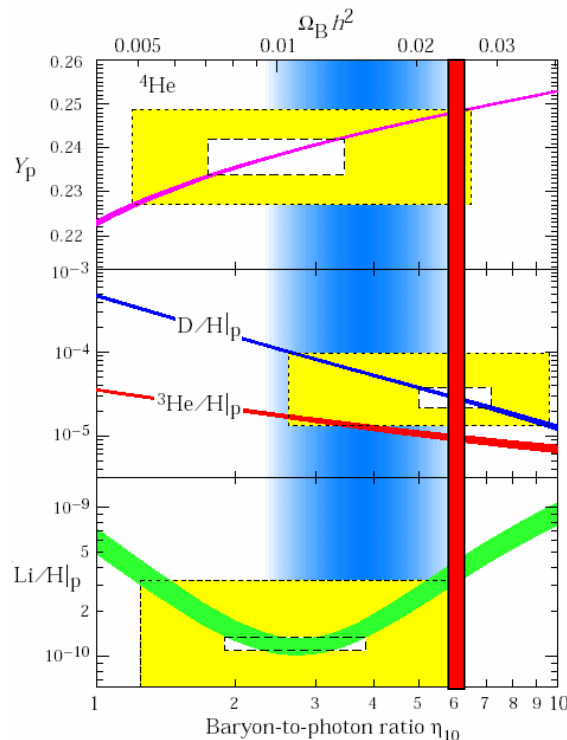
Dalcanton, Hogan (2000)
 Lin, Huang, Zhang, Brandenberger (2001)
 Sigurdson, Kamionkowski (2003)
 Profumo, Sigurdson, Ullio, Kamionkowski (2004)
 Kaplinghat (2005)
 Cembranos, Feng, Rajaraman, Takayama (2005)
 Strigari, Kaplinghat, Bullock (2006)
 Bringmann, Borzumati, Ullio (2006)



Kaplinghat (2005)

BIG BANG NUCLEOSYNTHESIS

Late decays may modify light element abundances



After WMAP

- $\eta_D = \eta_{\text{CMB}}$
- Independent ${}^7\text{Li}$ measurements are all low by factor of 3:

$${}^7\text{Li}/\text{H} = 1.5_{-0.5}^{+0.9} \times 10^{-10} \quad (95\% \text{ CL}) \quad [27]$$

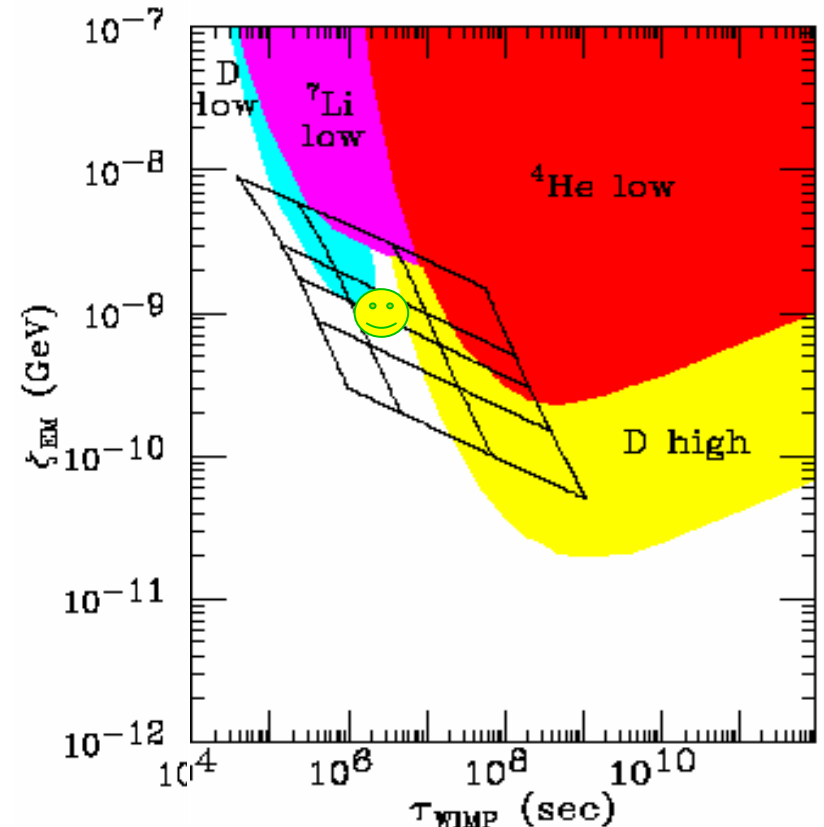
$${}^7\text{Li}/\text{H} = 1.72_{-0.22}^{+0.28} \times 10^{-10} \quad (1\sigma + \text{sys}) \quad [28]$$

$${}^7\text{Li}/\text{H} = 1.23_{-0.32}^{+0.68} \times 10^{-10} \quad (\text{stat} + \text{sys}, 95\% \text{ CL}) \quad [29]$$

Fields, Sarkar, PDG (2002)

BBN EM PREDICTIONS

- Consider $\tilde{\tau} \rightarrow \tilde{G} \tau$
- Grid: Predictions for
 $m_{\tilde{G}} = 100 \text{ GeV} - 3 \text{ TeV}$ (top to bottom)
 $\Delta m = 600 \text{ GeV} - 100 \text{ GeV}$ (left to right)
- Some parameter space excluded, but much survives
- SuperWIMP DM naturally explains ${}^7\text{Li}$!



Feng, Rajaraman, Takayama (2003)

BBN RECENT DEVELOPMENTS

- Much recent progress, results depend sensitively on what particle decays to gravitino.
- Hadronic decays are important
 - constrain $\chi \rightarrow Z \tilde{G} \rightarrow q q \tilde{G}$
 - Slepton, sneutrino decays ok

Kawasaki, Kohri, Moroi (2004); Jedamzik (2004); Feng, Su, Takayama (2004);
Jedamzik, Choi, Roszkowski, Ruiz de Austri (2005)

- Charged particles catalyze BBN: ${}^4\text{He } X^- + d \rightarrow {}^6\text{Li} + X^-$
 - Constrain $\tilde{\tau} \rightarrow \tilde{G} \tau$ to lifetimes $< 10^4$ seconds
 - Neutralino, sneutrino decays ok

Pospelov (2006); Kaplinghat, Rajaraman (2006); Kohri, Takayama (2006);
Cyburt, Ellis, Fields, Olive, Spanos (2006); Hamaguchi, Hatsuda, Kamimura, Kino, Yanagida (2007);
Bird, Koopmans, Pospelov (2007); Takayama (2007)

SUPERWIMPS AT COLLIDERS

- Each SUSY event may produce 2 metastable sleptons
Spectacular signature: slow, highly-ionizing charged tracks

Current bound (LEP): $m_{\tilde{\tau}} > 99 \text{ GeV}$

Tevatron reach: $m_{\tilde{\tau}} \sim 180 \text{ GeV}$ for 10 fb^{-1} (now?)

LHC reach: $m_{\tilde{\tau}} \sim 700 \text{ GeV}$ for 100 fb^{-1}

Drees, Tata (1990)

Goity, Kossler, Sher (1993)

Feng, Moroi (1996)

Hoffman, Stuart et al. (1997)

Acosta (2002)

...

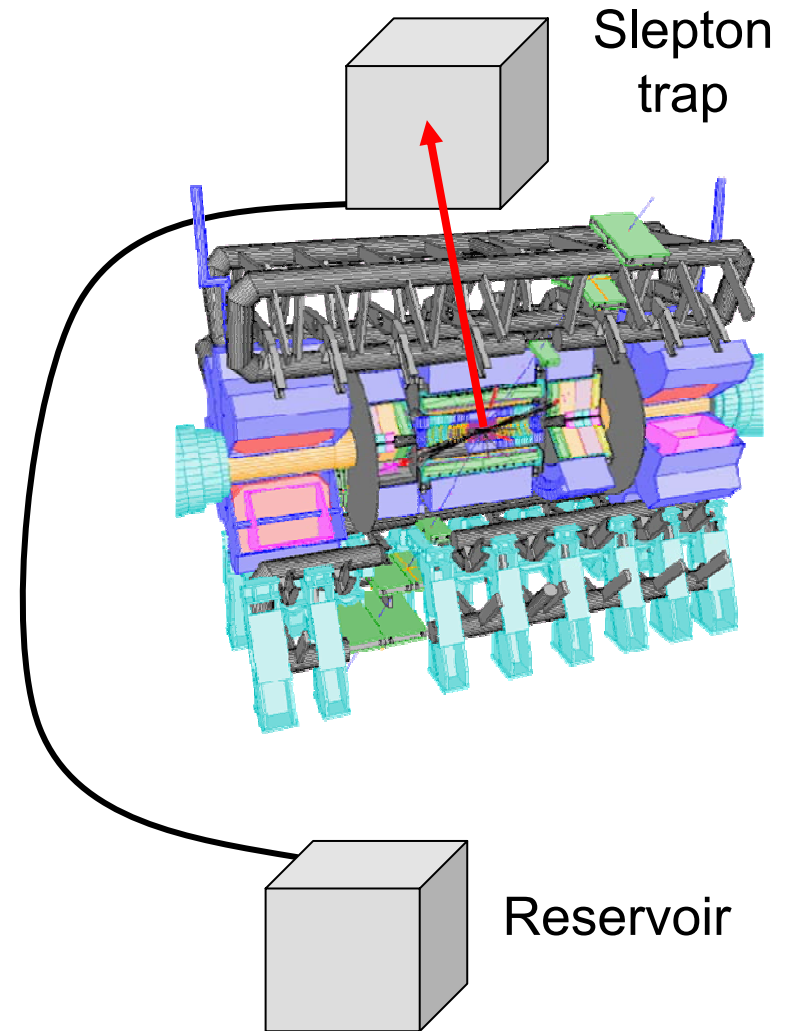
Slepton Trapping

- Sleptons can be trapped and moved to a quiet environment to study their decays
- Crucial question: how many can be trapped by a reasonably sized trap in a reasonable time?

Feng, Smith (2004)

Hamaguchi, Kuno, Nakawa, Nojiri (2004)

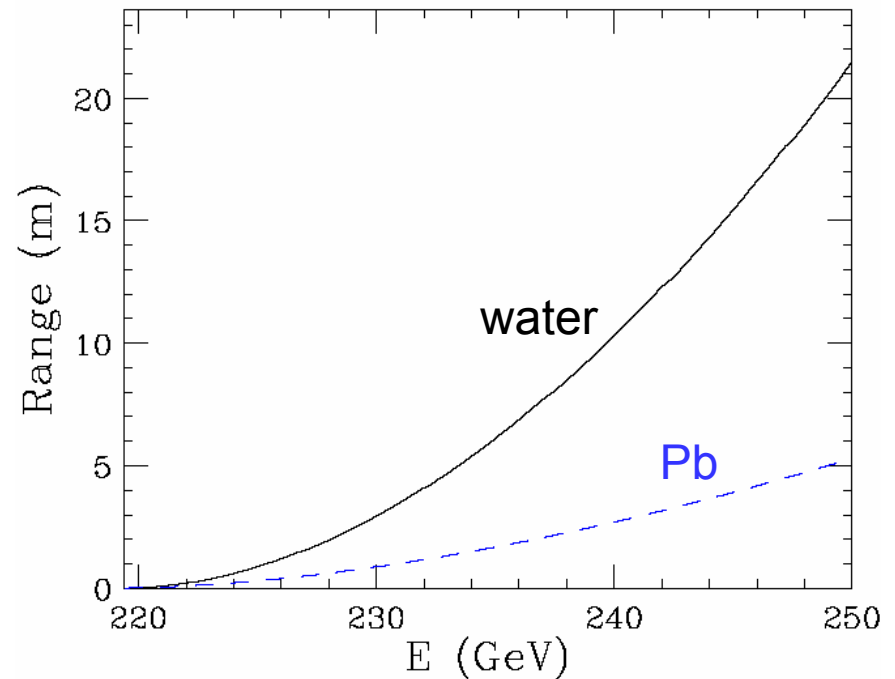
De Roeck et al. (2005)



Slepton Range

- Ionization energy loss described by Bethe-Bloch equation:

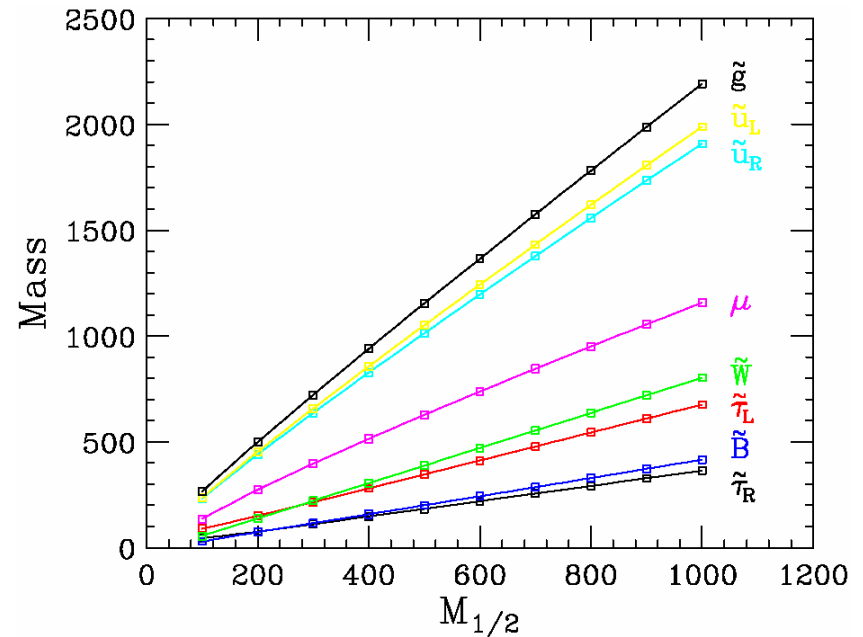
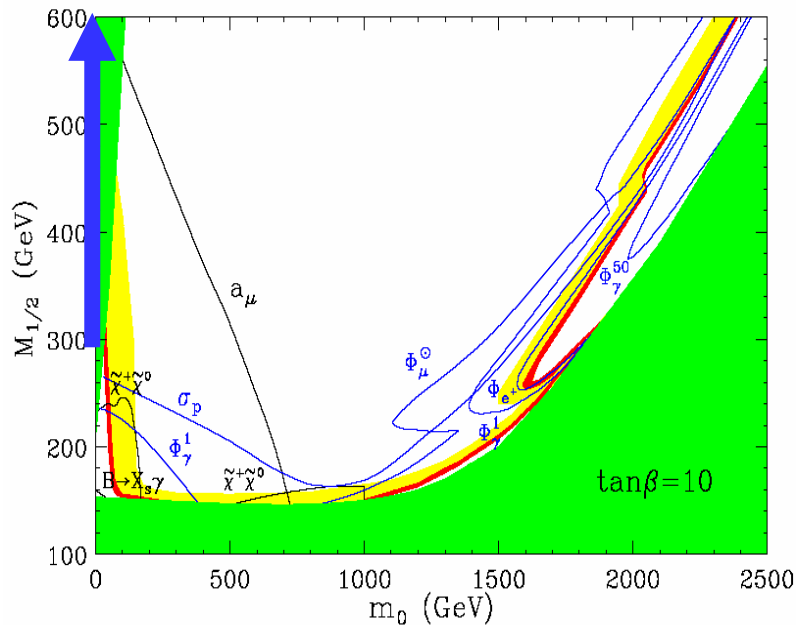
$$\frac{dE}{dx} = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\ln \left(\frac{2m_e c^2 \beta^2 \gamma^2}{I \sqrt{1 + \frac{2m_e \gamma}{M} + \frac{m_e^2}{M^2}}} \right) - \beta^2 - \frac{\delta}{2} \right]$$



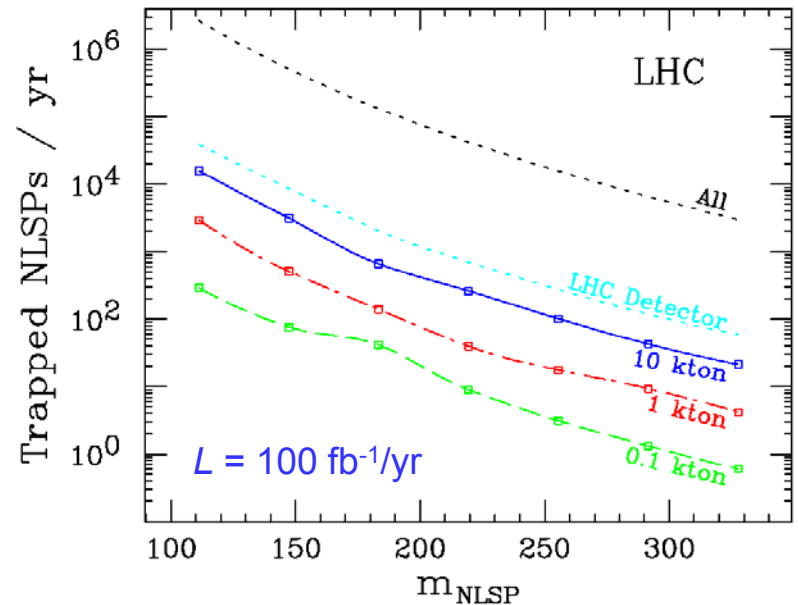
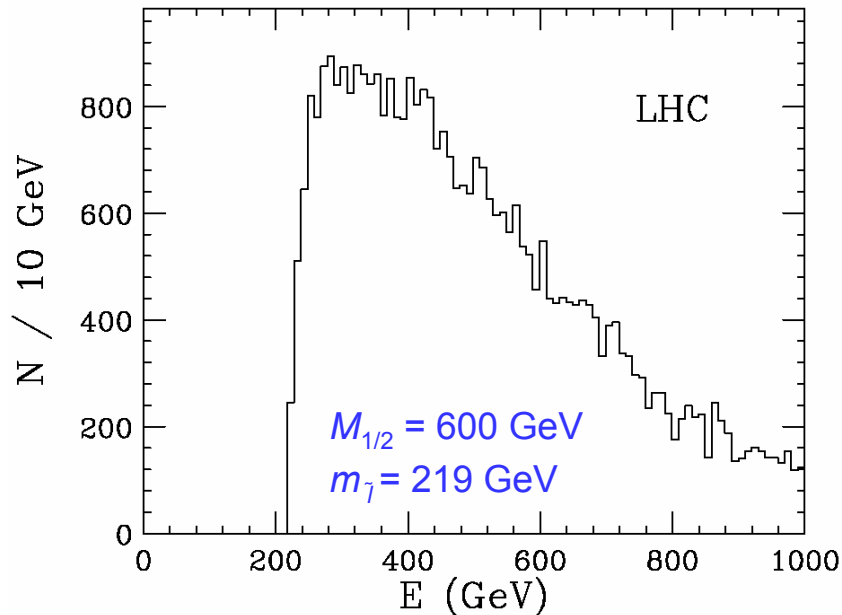
$$m_{\tilde{\gamma}} = 219 \text{ GeV}$$

Model Framework

- Results depend heavily on the entire SUSY spectrum
- Consider mSUGRA with $m_0=A_0=0$, $\tan\beta = 10$, $\mu>0$
 $M_{1/2} = 300, 400, \dots, 900$ GeV



Large Hadron Collider

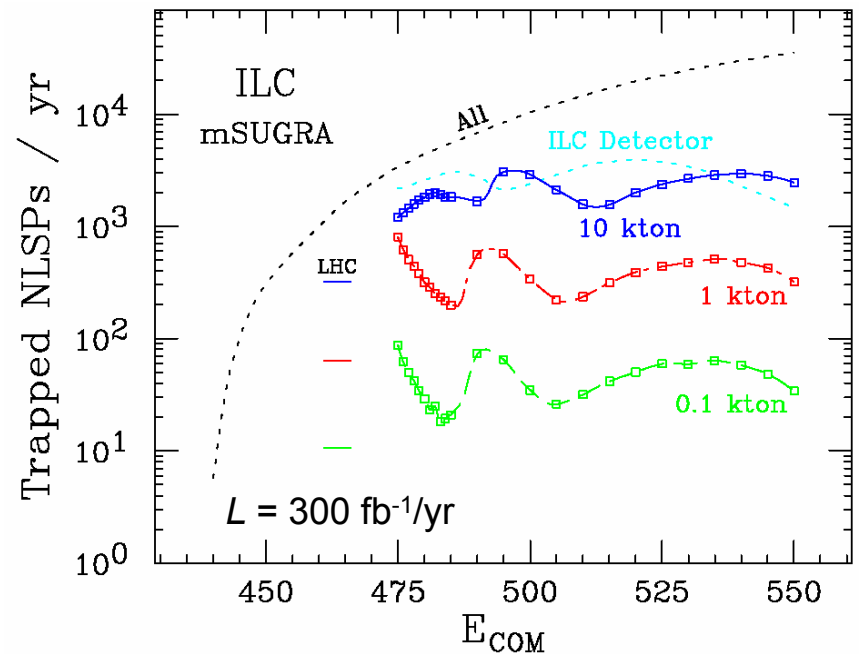
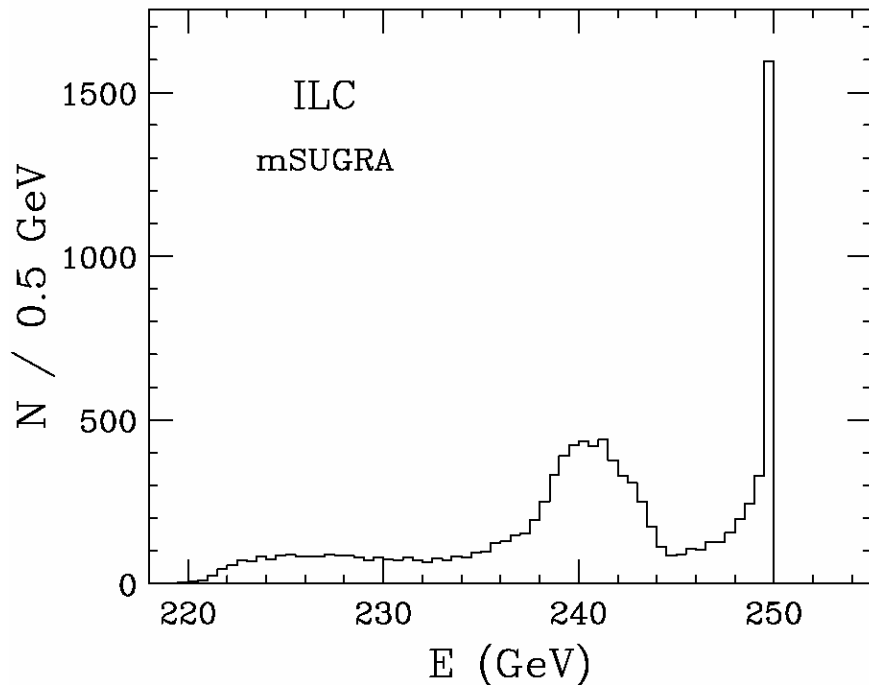


Of the sleptons produced, $O(1)\%$ are caught in 10 kton trap

10 to 10^4 trapped sleptons in 10 kton trap (1 m thick)

International Linear Collider

m_χ	242.9 GeV	} mSUGRA
$m_{\tilde{e}_R}, m_{\tilde{\mu}_R}$	227.2 GeV	
$m_{\tilde{\tau}_R}$	219.3 GeV	
		} NLSP only



Sleptons are slow, most can be caught in 10 kton trap
Factor of ~ 10 improvement over LHC

Measuring $m_{\tilde{G}}$ and M_*

- Decay width to \tilde{G} :

$$\Gamma(\tilde{\ell} \rightarrow \ell \tilde{G}) = \frac{1}{48\pi M_*^2} \frac{m_{\tilde{\ell}}^5}{m_{\tilde{G}}^2} \left[1 - \frac{m_{\tilde{G}}^2}{m_{\tilde{\ell}}^2} \right]^4$$

- Measurement of $\Gamma \rightarrow m_{\tilde{G}}$
 - $\Omega_{\tilde{G}}$. SuperWIMP contribution to dark matter
 - F . Supersymmetry breaking scale, dark energy
 - Early universe (BBN, CMB) in the lab
- Measurement of Γ and $E_l \rightarrow m_{\tilde{G}}$ and M_*
 - Precise test of supergravity: gravitino is graviton partner
 - Measurement of G_{Newton} on fundamental particle scale
 - Probes gravitational interaction in particle experiment

Hamaguchi et al. (2004); Takayama et al. (2004)

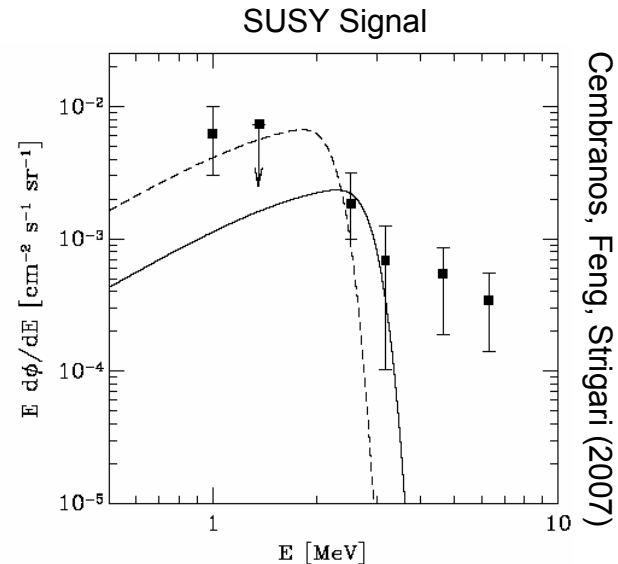
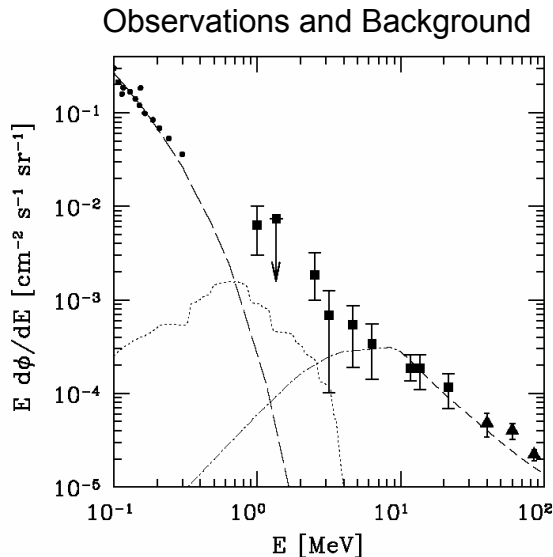
ARE WIMPS STABLE?

- Not necessarily. In fact, they can be decaying now:

$$\chi \rightarrow \gamma \tilde{G}$$

- Signals in the diffuse photon flux, completely determined by 1 parameter:

$$\tau \simeq \frac{3\pi}{b \cos^2 \theta_W} \frac{M_P^2}{(\Delta m)^3} \simeq \frac{4.7 \times 10^{22} \text{ s}}{b} \left[\frac{\text{MeV}}{\Delta m} \right]^3$$



CONCLUSIONS

- Weak-scale DM has never been more motivated
 - Cosmological legacy of LEP: stability of a new particle is common feature of viable particle models
- SUSY provides many well-motivated, and qualitatively different, candidates
 - WIMPs and superWIMPs
 - Cold and warm
 - Stable and metastable
- If anything mentioned here is correct, life will be very interesting in the coming years